

Thermodynamic Difference Rules: A Prescription for Their Application and Usage to Approximate Thermodynamic Data[†]

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Thermodynamic data are required for an understanding of the behavior of materials but are often lacking (or even unreliable) for a variety of reasons such as synthetic problems, purity issues, failure to correctly identify hydrolysis products, instability of the material, etc. Thus, it is necessary to develop procedures for the estimation of that data. The Thermodynamic Difference Rules (TDR) are additive approximations by which the properties of materials are estimated by reference to those of related materials. These rules appear in the form of the reliable Hydrate Difference Rule (HDR), based on the well-established properties of the large number of known hydrates, and the somewhat less certain Solvate Difference Rule (SDR). These rules are briefly surveyed and their application carefully delineated by a scheme and demonstrated by a number of calculated examples.

Introduction

It must be admitted that thermodynamic properties,¹ although useful, are frequently unavailable for the materials of importance in modern chemistry. Over three decades ago, O'Hare² drew attention to this shortfall of data when he noted that *high-tech* materials often have *low-tech* thermodynamics. The situation, far from improving, seems to have become even worse. Yet, in a climate of increasing demands on scientific resources worldwide, the prospect of the routine experimental determination of the key thermodynamic properties (i.e., $\Delta_f G^\circ$, $\Delta_f H^\circ$, and S°_{298})—much in the manner by which provision of crystallographic data is standard practice for newly synthesized materials—is unlikely to emerge on any foreseeable future scientific agenda. A convenient route out of this difficulty has seemed to us to devise procedures which could estimate thermodynamic data either relying on existing known thermodynamic information or derived from readily available *crystallographic* databases. The former development gave rise to the Thermodynamic (Hydrate and Solvate) Difference Rules (TDR),^{3–7} while the latter has resulted in our Volume-Based Thermodynamics (VBT) procedures^{8–20} (consideration of which will be deferred to a subsequent publication²¹).

These two approaches are gradually being adopted, the former (TDR) to provide data for modern synthetic reactions taking place within nonaqueous media⁷ and the latter (VBT) to provide a whole range of applications in areas where no thermodynamic data are otherwise available. Some progress is currently being made toward the expansion of the thermodynamic property database, but increasingly, this is not from experimental sources. Instead, data are being provided by quantum chemical calculations^{22–27} and by empirical^{28–31} and group contribution

methods^{32–34}—where we have simply noted just a few representative examples. Papers reporting thermochemical data based solely on calorimetric measurements are proportionately fewer with time, contrasted with the increasing proportion of those emerging from quantum chemical and other theoretical methods, of one variety or another.

We review briefly our contributions through the Thermodynamic Difference Rules, which are forms of the additivity rule. They comprise a rule for hydrate salts (the Hydrate Difference Rule, HDR) which works very satisfactorily and a rule for inorganic solvate systems, more generally, the Solvate Difference Rule (SDR), currently still very much under development. The latter rule is subject to greater uncertainties pending further data generation by experimental or other means. Indeed, Fyfe et al.³⁵ have earlier noted that "... if both heats and entropies were exactly additive, [Gibbs] energies would also be additive, and the [Gibbs]-energy change for any reaction between such compounds should be zero... More generally, if the additivity rule were exactly obeyed, all phases would always be in equilibrium...".

We provide a flow-chart (Scheme 1) enabling these TDR procedures to be easily understood and used by occasional users and nonexperts wishing to introduce, perhaps for the first time, thermodynamic arguments in support of their results.

Our procedures are such that they can also be used to provide speculative thermodynamic data for hypothetical, as yet unprepared, materials as well as for those that are challenging to handle experimentally, being unstable, radioactive, or hygroscopic.

Thermodynamic Difference Rule (TDR) Procedures. In its most important role, the TDR^{3–7} is designed to provide a means whereby new thermodynamic data can be inferred from established data. We examine its credentials by considering separately the hydrate ($M_p X_q \cdot nH_2O$) and solvate ($M_p X_q \cdot nS$) difference rules. We list and examine the use of various relationships which we have developed and demonstrate their use both for the validation of existing data when choices are possible and in checking the consistency of data sets.

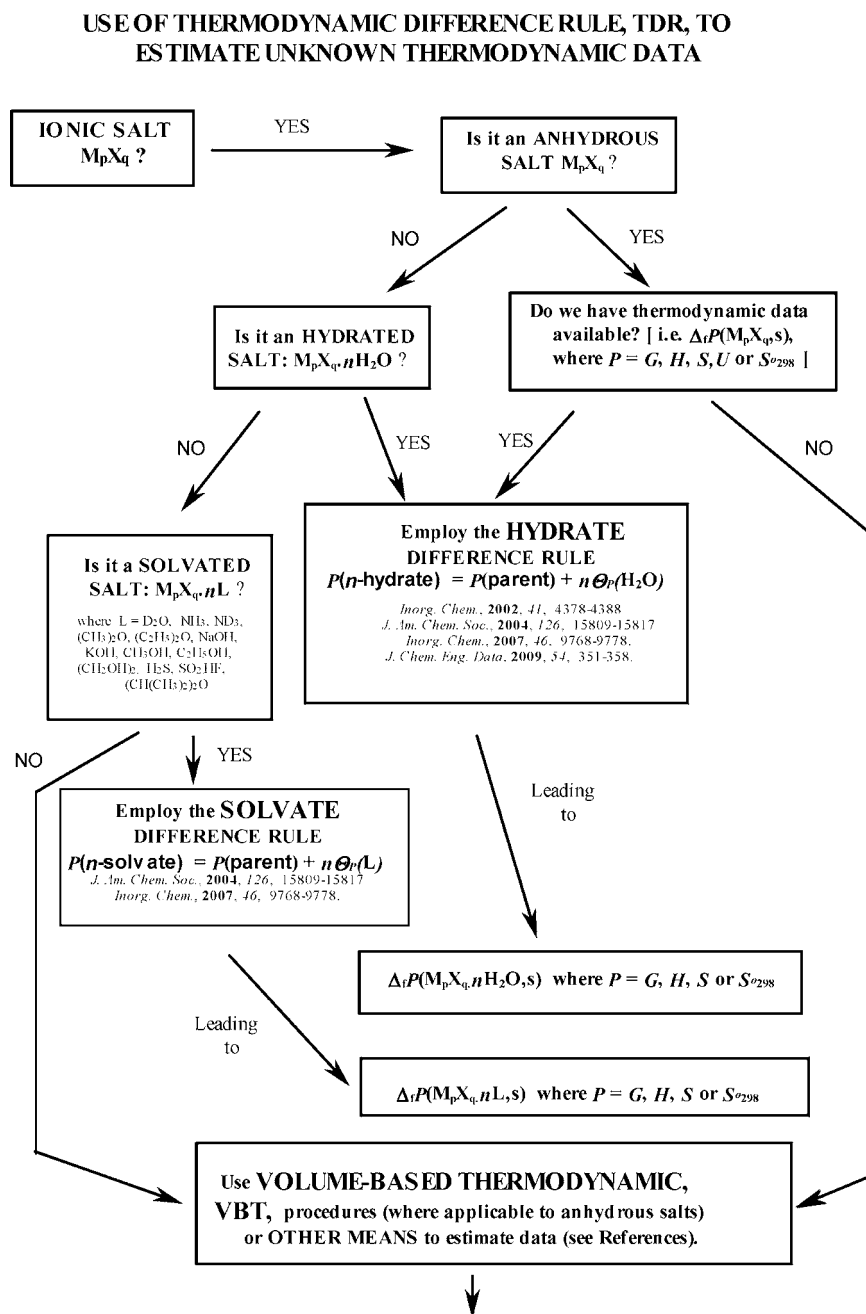
[†] Part of the "Sir John S. Rowlinson Festschrift".

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Scheme 1



This paper simplifies notation wherever possible. More details can be found in the main papers,³⁻⁶ while Table 1 provides the key.

$$P(n\text{-hydrate}) \approx P(\text{parent}) + n\theta_p(\text{H}_2\text{O}) \quad (1)$$

$$[P(m\text{-hydrate}) - P(n\text{-hydrate})] \approx (m-n)\theta_p(\text{H}_2\text{O}) \quad (2)$$

$$P(k\text{-hydrate}) + P(l\text{-hydrate}) \approx P(m\text{-hydrate}) + P(n\text{-hydrate}) \quad \text{with } k + l = m + n \quad (3)$$

$$P(k\text{-hydrate}) + P(l\text{-hydrate}') \approx P(m\text{-hydrate}) + P(n\text{-hydrate}') \quad \text{with } k + l = m + n \quad (4)$$

where these equations, which are simply variations of one another, are expressions of the additivity of corresponding thermodynamic properties, as defined in Table 1, top of third column. Equation 2 follows directly from eq 1.

θ_p values are reasonably constant throughout for all hydrates (whether single or complex), with the values being well

established for the standard thermodynamic properties: $\Delta_f H^\circ$, $\Delta_f G^\circ$, and S°_{298} .

$$\theta_{\text{Hf}}(\text{H}_2\text{O})/\text{kJ}\cdot\text{mol}^{-1} \approx -298.6 \quad (5)$$

$$\theta_{\text{Gf}}(\text{H}_2\text{O})/\text{kJ}\cdot\text{mol}^{-1} \approx -242.4 \quad (6)$$

$$\theta_s(\text{H}_2\text{O})/\text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1} \approx 40.9 \quad (7)$$

Usage of HDR Equations

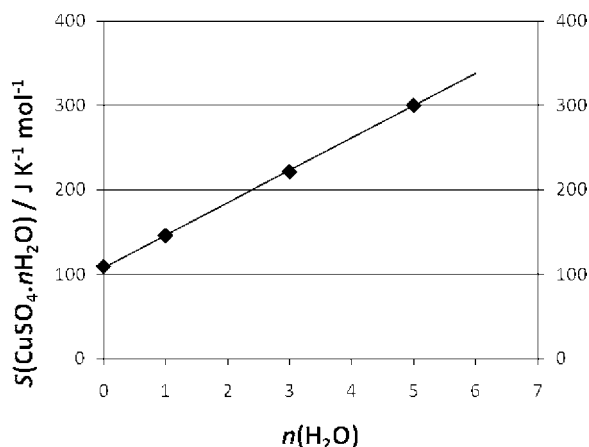
Usage is illustrated by several practical examples.

Example 1: Standard Entropy Estimation. The NBS database³⁶ lists the standard entropy for copper sulfate monohydrate, $S^\circ_{298}(\text{CuSO}_4\cdot\text{H}_2\text{O}, \text{s})/\text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$, to be 146.0. Predict the standard entropies, $S^\circ_{298}(\text{CuSO}_4\cdot n\text{H}_2\text{O}, \text{s})$, of the 3, 5, and 6 hydrates and of the parent, $S^\circ_{298}(\text{CuSO}_4, \text{s})$.

From eq 1, using $\theta_s(\text{H}_2\text{O})$ from eq 7, $S^\circ_{298}(n\text{-hydrate}) \approx S^\circ_{298}(\text{parent}) + 40.9n$, so, rearranging, we predict that

Table 1. Simplified Notation Used in the Current Paper

full notation as used in main papers ³⁻⁶	notation adopted here	interpretation
$P(M_p X_q, s)$	$P(\text{parent}) \equiv P(\theta\text{-hydrate})$	P represents the thermodynamic property under consideration, which may be standard enthalpy of formation, Gibbs energy of formation, or standard entropy. $M_p X_q$ represents an inorganic salt in the crystalline state (s). $M'_p X'_q$ represents a different inorganic salt, distinguishable from $M_p X_q$. Unsolvated/anhydrous materials are distinguished as parent and parent'. L represents a nonaqueous solvent. H_2O represents specifically water. θ_P represents a constant property contribution whose value is appropriate to the property P being investigated, the solvent L involved (water for hydrates), and the physical states of the solvate/hydrate and parent salts considered, most usually solids (s), hence s-s.
$P(M_p X_q \cdot nH_2O, s)$	$P(n\text{-hydrate})$	
$P(M'_p X'_q \cdot nH_2O, s)$	$P(n\text{-hydrate}')$	
$P(M_p X_q \cdot nL, s)$	$P(n\text{-solvate})$	
$P(M'_p X'_q \cdot nL, s)$	$P(n\text{-solvate}')$	
$P(M_p X_q, s)$	$P(\text{parent}') \equiv P(\theta\text{-hydrate}')$	
$\theta_P(H_2O, s-s)$	$\theta_P(H_2O)$	$\theta_{Hf}(H_2O)/kJ \cdot mol^{-1} \approx -298.6$ $\theta_{Gf}(H_2O)/kJ \cdot mol^{-1} \approx -242.4$ $\theta_S(H_2O)/J \cdot K^{-1} \cdot mol^{-1} \approx 40.9$
$\theta_P(L, s-s)$	$\theta_P(L)$	Values for $\theta_P(L)$ for a limited number of solvents, L , and properties P are listed in Table 1 of ref 4.

**Figure 1.** HDR of $S^\circ_{298}(n\text{-hydrate}, s)$ for $CuSO_4$ versus $n(H_2O)$. The least-squares fitted line has the equation $S^\circ_{298}(n\text{-hydrate}, s)/J \cdot K^{-1} \cdot mol^{-1} \approx 38.2n + 108.3$ ($R^2 = 0.9998$, $N = 4$).

$$S^\circ_{298}(CuSO_4, s)/J \cdot K^{-1} \cdot mol^{-1} \approx 146.0 - 40.9 = 105.1 \text{ (} 109.3 \pm 0.4^{37} \text{ 3.8 \%)}$$

$$S^\circ_{298}(CuSO_4 \cdot 3H_2O, s)/J \cdot K^{-1} \cdot mol^{-1} \approx 227.8 \text{ (} 221.3, \text{ 2.9 \%)}$$

$$S^\circ_{298}(CuSO_4 \cdot 5H_2O, s)/J \cdot K^{-1} \cdot mol^{-1} \approx 309.6 \text{ (} 300.4, \text{ 3.1 \%)}$$

and

$$S^\circ_{298}(CuSO_4 \cdot 6H_2O, s)/J \cdot K^{-1} \cdot mol^{-1} \approx 350.5$$

Comparison with experimental values (in parentheses), known for $n = 3$ and 5, leads to the errors listed. $S^\circ_{298}(CuSO_4 \cdot 6H_2O, s)/J \cdot K^{-1} \cdot mol^{-1}$ has not been recorded, and this prediction should be good to (approximately) $\pm 15 J \cdot K^{-1} \cdot mol^{-1}$. It should be mentioned that, if one is wishing to predict a value for a hydrate within a family of hydrates for which experimental values are known for several members of the series, then the preferred route would be to plot the specific experimental $P(n\text{-hydrate}, s)$ values.

Thus, for the $n = 0, 1, 3,$ and 5 hydrates, a plot of $S^\circ_{298}(CuSO_4 \cdot nH_2O, s)/J \cdot K^{-1} \cdot mol^{-1}$ versus n leads (Figure 1) to eq 8 from which we can predict a more likely hexahydrate entropy, based on the series concerned rather than the general θ values

$$S^\circ_{298}(CuSO_4 \cdot nH_2O, s)/J \cdot K^{-1} \cdot mol^{-1} \approx 38.2n + 108.3 \quad (R^2 = 0.9998, N = 4) \quad (8)$$

$$S^\circ_{298}(CuSO_4 \cdot 6H_2O, s)/J \cdot K^{-1} \cdot mol^{-1} \approx 337.5$$

An approximate hydrate entropy value can also be estimated using Latimer's additive approach,^{38,39} from which $S^\circ_{298}(CuSO_4 \cdot 6H_2O, s)/J \cdot K^{-1} \cdot mol^{-1} \approx 45.2 + 72.0 + 6(39.3) = 353.2$.

Example 2: Gibbs Energy Estimation. The NBS database³⁶ lists the standard Gibbs energy of formation, $\Delta_f G^\circ$, for the parent and three hydrates of $ZnSO_4 \cdot nH_2O$ (Table 2). Using the end members ($n = 0$ and 7), use eq 2 to estimate $\theta_{Gf}(H_2O)/kJ \cdot mol^{-1}$. (Our generic value, eq 6, is $-242.4 kJ \cdot mol^{-1}$.)

Table 2. Gibbs Energy of Formation, $\Delta_f G^\circ$, for the Parent and Three Hydrates of $ZnSO_4 \cdot nH_2O$

n	0	1	6	7
$\Delta_f G^\circ/kJ \cdot mol^{-1}$	-871.5	-1131.99	-2324.44	-2562.67

Using eq 2 ($P = \Delta_f G^\circ$) and the end members

$$\theta_{Gf}(H_2O)/kJ \cdot mol^{-1} \approx$$

$$[P(7\text{-hydrate}) - P(\text{parent})]/(7 - 0) = [-2562.67 + 871.5]/7 = -241.6 \text{ (} 0.3 \% \text{)}$$

A more suitable alternative strategy is to plot the data versus n , as shown in Figure 2. The linear fit takes the analytical form

$$\Delta_f G^\circ(n\text{-hydrate}, s)/kJ \cdot mol^{-1} \approx -240.6n - 880.7 \quad (R^2 = 0.999, N = 4) \quad (9)$$

from which we infer for $ZnSO_4$ hydrates that

$$\theta_{Gf}(H_2O)/kJ \cdot mol^{-1} \approx -240.6 \text{ (} 0.8 \% \text{)}$$

Example 3. Example 3 shows that the experimental data for $ZnSO_4$ hydrate in Table 2 above fits eq 3 under the condition that $k + l = m + n$.

Taking $k = 0, l = 7, m = 1,$ and $n = 6,$ satisfying the condition, the data show that

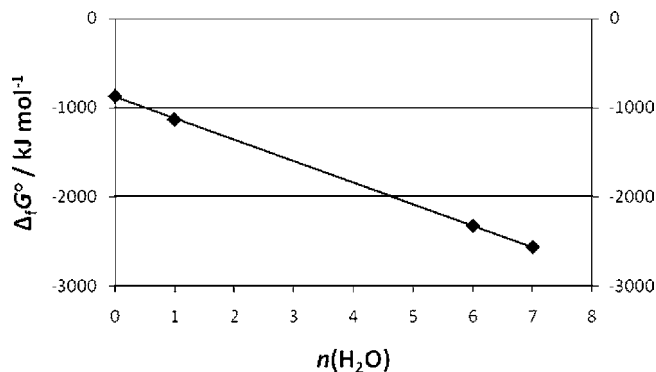


Figure 2. HDR of $\Delta_r G^\circ(n\text{-hydrate, s})/\text{kJ}\cdot\text{mol}^{-1}$ for ZnSO_4 versus $n(\text{H}_2\text{O})$. The least-squares fitted line has the equation $\Delta_r G^\circ(n\text{-hydrate, s})/\text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1} = -240.6n - 880.7$ ($R^2 = 0.999$, $N = 4$).

Table 3. Enthalpies of Formation, $\Delta_f H^\circ$, for the Parents and Hydrates of MgSO_4 and of MgSeO_4 , from Different Sources

$\Delta_f H^\circ(n\text{-hydrate, s})$	$\text{kJ}\cdot\text{mol}^{-1}$		
	K&K ^{40,42,43}	K&K ^{40,42,44}	NBS ³⁶
MgSO_4	-1301.43	-1301.43	-1284.9
$\text{MgSO}_4\cdot\text{H}_2\text{O}$	-1278.2	-1604.6	-1602.1
$\text{MgSO}_4\cdot 1.25\text{H}_2\text{O}$	-1673.2	-1671.1	
$\text{MgSO}_4\cdot 1.5\text{H}_2\text{O}$	-1753.5	-1748.5	
$\text{MgSO}_4\cdot 2\text{H}_2\text{O}$	-1953.9	-1943.9	-1896.2
$\text{MgSO}_4\cdot 3\text{H}_2\text{O}$	-2210.4	-2200.8	
$\text{MgSO}_4\cdot 4\text{H}_2\text{O}$	-2530.9	-2520	-2496.6
$\text{MgSO}_4\cdot 5\text{H}_2\text{O}$			-2795.75
$\text{MgSO}_4\cdot 6\text{H}_2\text{O}$	-3104.1	-3084.4	-3087
$\text{MgSO}_4\cdot 7\text{H}_2\text{O}$	-3376.5	-3366.9	-3388.7
MgSeO_4	-983.32	-999	-968.5
$\text{MgSeO}_4\cdot\text{H}_2\text{O}$	-1312.43	-1310.26	-1295.45
$\text{MgSeO}_4\cdot 4\text{H}_2\text{O}$	-2204.47	-2204.8	-2189.91
$\text{MgSeO}_4\cdot 6\text{H}_2\text{O}$	-2835.41	-2793.9	-2779

Table 4. Optimized Enthalpies of Formation, $\Delta_f H^\circ$, for the Parents and Hydrates of MgSO_4 and of MgSeO_4 , Using the Different Sources for Reference

sum of squares of errors	96844	3019	661
	% diff K&K ^{40,42,43}	% diff K&K ^{40,42,44}	% diff NBS ³⁶
MgSO_4	4.3	-0.8	-0.7
$\text{MgSO}_4\cdot\text{H}_2\text{O}$	-21.7	-0.2	0.5
$\text{MgSO}_4\cdot 1.25\text{H}_2\text{O}$	2.4	-0.7	(-1668.4) ^a
$\text{MgSO}_4\cdot 1.5\text{H}_2\text{O}$	2.5	-0.5	(-1743.3) ^a
$\text{MgSO}_4\cdot 2\text{H}_2\text{O}$	4.6	2.0	0.2
$\text{MgSO}_4\cdot 3\text{H}_2\text{O}$	1.6	0.0	(-2193.1) ^a
$\text{MgSO}_4\cdot 4\text{H}_2\text{O}$	1.9	0.9	0.1
$\text{MgSO}_4\cdot 5\text{H}_2\text{O}$	-	-	0.1
$\text{MgSO}_4\cdot 6\text{H}_2\text{O}$	0.0	-0.2	-0.2
$\text{MgSO}_4\cdot 7\text{H}_2\text{O}$	-1.1	-0.6	-0.1
MgSeO_4	0.0	-1.2	-1.6
$\text{MgSeO}_4\cdot\text{H}_2\text{O}$	1.5	0.2	0.9
$\text{MgSeO}_4\cdot 4\text{H}_2\text{O}$	-0.7	0.3	0.3
$\text{MgSeO}_4\cdot 6\text{H}_2\text{O}$	-0.2	0.1	-0.1

^a The formation enthalpies in parentheses are calculated for the missing entries in the NBS tables.

$$[P(k\text{-hydrate}) + P(l\text{-hydrate})]/\text{kJ}\cdot\text{mol}^{-1} = [P(0\text{-hydrate}) + P(7\text{-hydrate})] = -3434.2$$

and that

$$[P(l\text{-hydrate}) + P(m\text{-hydrate})]/\text{kJ}\cdot\text{mol}^{-1} = [P(1\text{-hydrate}) + P(6\text{-hydrate})] = -3456.4$$

and hence that, to within 0.6 %, eq 3 is valid.

Example 4: Consistency Check of Data. The NBS³⁶ and Karapet'yants and Karapet'yants⁴⁰⁻⁴³ tabulations cite differing values for the MgSO_4 and MgSeO_4 parent and hydrate enthal-

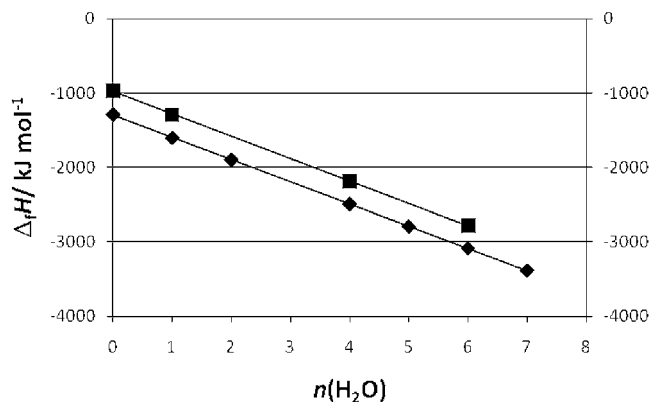


Figure 3. HDR of $\Delta_r H^\circ(n\text{-hydrate, s})/\text{kJ}\cdot\text{mol}^{-1}$ for MgSO_4 and its hydrates (diamonds) and MgSeO_4 and its hydrates (squares) versus $n(\text{H}_2\text{O})$. The slopes of linear plots are $(-299.5$ and $-298.8)$ $\text{kJ}\cdot\text{mol}^{-1}$, respectively.

pies, as in Table 3. We investigate which set of data is most self-consistent.

Table 4 shows the results of application of the Excel "Solver" optimization routine (see Supporting Information) using the columns of enthalpy data from the table above and allowing Solver to optimize simultaneously the enthalpy contributions of H_2O , MgSO_4 , and MgSeO_4 . (Solver operates in this instance by minimizing the sum-of-squares difference between the literature formation enthalpies and those calculated from a starting set of enthalpies for the component species (H_2O , MgSO_4 , and MgSeO_4), by adjusting the latter values.) Quite clearly, the NBS data set is most suitable, with $\Delta_f H^\circ(\text{H}_2\text{O, s}) = -299.9$, $\Delta_f H^\circ(\text{MgSO}_4, \text{s}) = -1293.6$, and $\Delta_f H^\circ(\text{MgSeO}_4, \text{s}) = -983.6$ $\text{kJ}\cdot\text{mol}^{-1}$.

From Figure 3, the slopes of enthalpy versus $n(\text{H}_2\text{O})$ linear plots are -299.4 and -298.8 $\text{kJ}\cdot\text{mol}^{-1}$, for MgSO_4 and MgSeO_4 hydrates, respectively, compared with the best optimized value of -299.9 $\text{kJ}\cdot\text{mol}^{-1}$ noted above, and the generalized value of $\theta_{\text{Hf}}(\text{H}_2\text{O}) = -298.6$ $\text{kJ}\cdot\text{mol}^{-1}$ from eq 5.

Example 5: Do the Hydrates Formed by Salts of Organic Acids Obey the Difference Rule? The number of hydrate examples of organic acids for which thermodynamic data are available is somewhat limited. To examine this question, in Table 5 we cite examples of $\Delta_f H^\circ$ for some organic acid salts as given in the NBS tables³⁶ and use the Thermodynamic Difference Rule, taking $\theta_{\text{Hf}}(\text{H}_2\text{O, s-s}) = -298.6$ $\text{kJ}\cdot\text{mol}^{-1}$ to predict the hydrate value from the given parent entry. The final column shows the % error, from which we see that the rule does enable estimation of this data, usually to within experimental error.

HDR Errors. Experimental values^{36,40} for $\Delta_f G^\circ(\text{MgSO}_4\cdot 6\text{H}_2\text{O, s})/\text{kJ}\cdot\text{mol}^{-1}$, to take an example of a typical hydrate, exhibit a range of 21 $\text{kJ}\cdot\text{mol}^{-1}$ (a range of 1 %), from -2603.7 to -2628.64 . This degree of uncertainty is often comparable with the errors arising from HDR predictions, rendering the latter extremely useful. In our previous studies, it was recorded that $\Delta_f G^\circ$ was predicted to within less than 1 % of the accepted value in 88 % of cases.

Solvate Difference Rule (SDR).

$$P(n\text{-solvate}) \approx P(\text{parent}) + n\theta_p(\text{L}) \quad (10)$$

$$[P(m\text{-solvate}) - P(n\text{-solvate})] \approx (m - n)\theta_p(\text{L}) \quad (11)$$

$$P(k\text{-solvate}) + P(l\text{-solvate}) \approx P(m\text{-solvate}) + P(n\text{-solvate}) \quad (12)$$

and more detailed rules involving change of parent and/or solvent

$$P(M_p X_q \cdot kL, s) + P(M'_p X'_q \cdot lL', s) \approx P(M_p X_q \cdot lL', s) + P(M'_p X'_q \cdot kL, s) \quad (13)$$

$$P(M_p X_q \cdot kL, s) + P(M'_p X'_q, s) \approx P(M_p X_q, s) + P(M'_p X'_q \cdot kL, s) \quad (14)$$

$$P(M_p X_q \cdot kL, s) + P(M'_p X'_q \cdot lL, s) \approx P(M_p X_q \cdot mL, s) + P(M'_p X'_q \cdot nL, s) \quad (15)$$

Further, if L' is specifically H_2O , then

$$P(M_p X_q \cdot kL, s) + P(M'_p X'_q \cdot lH_2O, s) \approx P(M_p X_q \cdot lH_2O, s) + P(M'_p X'_q \cdot kL, s) \quad (16)$$

where eq 11 derives directly from eq 10. In eqs 12 and 15, the condition $k + l = m + n$ must hold.

There are several general observations to be made at the outset with regard to $\Delta_f H^\circ$, $\Delta_f G^\circ$, and S°_{298} data for nonaqueous solvates, $M_p X_q \cdot nL$:

(1) Thermodynamic data available for solvates are generally sparse;

(2) Multiple determination of identical thermodynamic data is infrequent (so errors are difficult to quantify). This is an area which could do with further experimental work.

(3) Often, only $\Delta_f H^\circ(M_p X_q \cdot nL, s)$ experimental values are available⁶ (e.g., for solvents $L = D_2O$, $(C_2H_5)_2O$, $NaOH$, CH_3OH , C_2H_5OH , $(CH_2O)_2$, H_2S , and SO_2) and then often for very few compounds (3, 4, 3, 5, 11, 4, 4, and 9 respectively, for the solvents listed). Even with such limited data, correlation coefficients tend to be large, suggesting that SDR does apply.

(4) In very few cases ($L = NH_3$, ND_3 , $(CH_3)_2O$) are experimental values of $\Delta_f G^\circ(M_p X_q \cdot nL, s)$ and $S^\circ_{298}(M_p X_q \cdot nL, s)$ available and then in limited numbers, (4, 3, and 3) and (9, 3, and 3), respectively.

All of these factors lead to the result that the SDR is less accurate than the HDR in its predictions: HDR correlation coefficients are generally high, with large numbers of data sets (for $\Delta_f H^\circ$, $R^2 = 0.999$, $N = 342$; for $\Delta_f G^\circ$, $R^2 = 0.998$, $N = 93$; and for S°_{298} , $R^2 = 0.978$, $N = 83$), while those for SDR are generally much lower—even for $L = NH_3$, for which there are 270 ammoniates for which $\Delta_f H^\circ$ has been experimentally

determined, the correlation coefficient is $R^2 = 0.932$. Having said this though, statistics does tell us that the probability that this correlation is due simply to chance is less than one in a million! Still, circumspection is the order of the day with regard to the use of SDR, as the following examples reveal.

Usage of SDR Equations

Example 6. There is considerable uncertainty concerning the formation enthalpies of the indium trihalides, as follows: $\Delta_f H^\circ(\text{InX}_3, s)/\text{kJ}\cdot\text{mol}^{-1}$ for which values are -527.2 ,⁴⁰ -537.2 ³⁶ ($X = \text{Cl}$); -418.4 ,⁴⁰ -428.9 ³⁶ ($X = \text{Br}$); and -248.9 ,⁴⁰ -238.0 ³⁶ ($X = \text{I}$). We investigate the application of these SDR data to the indium trihalide *ammoniates*, using the data in Table 6 below.

In accordance with eqs 10 and 11, a plot is made of $P(n\text{-solvate})$ versus $n(\text{NH}_3)$ using the data displayed in Table 6. Figure 4 shows this plot where the linear analytical fits take the forms below (correlation coefficients in parentheses)

$$\Delta_f H^\circ(\text{InCl}_3 \cdot n\text{NH}_3, s)/\text{kJ}\cdot\text{mol}^{-1} = -92.10n - 622.7 \quad (\text{Diamonds}, R^2 = 0.985)$$

$$\Delta_f H^\circ(\text{InBr}_3 \cdot n\text{NH}_3, s)/\text{kJ}\cdot\text{mol}^{-1} = -94.22n - 518.6 \quad (\text{Squares}, R^2 = 0.985)$$

$$\Delta_f H^\circ(\text{InI}_3 \cdot n\text{NH}_3, s)/\text{kJ}\cdot\text{mol}^{-1} = -90.70n - 344.3 \quad (\text{Triangles}, R^2 = 0.988)$$

giving rise to an average value for $\theta_{\text{HF}}(\text{NH}_3)$ of

$$\theta_{\text{HF}}(\text{NH}_3)/\text{kJ}\cdot\text{mol}^{-1} \approx -92.3$$

which is some 14 % different than our global value of $-105.5 \text{ kJ}\cdot\text{mol}^{-1}$ cited in Table 1 of ref 4 but exactly matches the minimum incorporation enthalpy more recently observed.⁴⁴ It should be noted that the intercepts give poor representation of the $\Delta_f H^\circ(\text{InX}_3, s)/\text{kJ}\cdot\text{mol}^{-1}$ values. Errors here are 16 % ($X = \text{Cl}$), 21 % ($X = \text{Br}$), and 45 % ($X = \text{I}$).

This deserves some comment. The selection of only indium trihalide data for these specific plots would have been expected to provide a more appropriate value for $\theta_{\text{HF}}(\text{NH}_3)$ —optimized

Table 5. Formation Enthalpies of Organic Acid Salts and Their Hydrates, Predicted Enthalpies of Their Hydrates, and Percentage Errors

organic acid salt and hydrate(s)	$\Delta_f H^\circ$ kJ·mol ⁻¹	value predicted from the difference rule = parent value + $n\theta_{\text{HF}}(\text{H}_2\text{O}, s-s)$	% error
Bioxalate Salts and Double Oxalate Salts			
NaHC ₂ O ₄ (s)	-1082.0		
NaHC ₂ O ₄ ·H ₂ O (s)	-1384.1	-1380.6	0.2
KHC ₂ O ₄ ·H ₂ C ₂ O ₄ (s)	-1951.0		
KHC ₂ O ₄ ·H ₂ C ₂ O ₄ ·2H ₂ O (s)	-2533.0	-2548.2	0.6
Acetate Salts			
Sr(CH ₃ COO) ₂ (s)	-1487.4		
Sr(CH ₃ COO) ₂ ·1/2H ₂ O (s)	-1631.8	-1636.7	0.3
Ca(CH ₃ COO) ₂ (s)	-1479.5		
Ca(CH ₃ COO) ₂ ·H ₂ O (s)	-1772.3	-1778.1	0.3
Glycolate Salts			
CH ₂ OH·COONa (s)	-900.8		
CH ₂ OH·COONa·1/2H ₂ O(s)	-1048.9	-1050.1	0.1
CH ₂ OH·COOK (s)	-907.9		
CH ₂ OH·COOK·1/2H ₂ O (s)	-1064.4	-1057.2	0.7
Ca(CH ₂ OH·COO) ₂ (s)	-1856.0		
Ca(CH ₂ OH·COO) ₂ ·3H ₂ O (s)	-2736.3	-2751.8	0.6
Ca(CH ₂ OH·COO) ₂ ·5H ₂ O (s)	-3311.2	-3349.0	1.1
Sodium Disodium Hydroxyacetate			
NaOCH ₂ CO ₂ Na (s)	-1037.2		
NaOCH ₂ CO ₂ Na·2H ₂ O (s)	-1649.3	-1634.4	0.9

Table 6. Results for Linear SDR Plots for Ammoniates of Indium Trihalides, InX_3 (X = Cl, Br, I)^a

<i>n</i>	experimental			predictions and % errors					
	$\Delta_f H^\circ$ X = Cl	$\Delta_f H^\circ$ X = Br	$\Delta_f H^\circ$ X = I	$\Delta_f H^\circ$ X = Cl	% error	$\Delta_f H^\circ$ X = Br	% error	$\Delta_f H^\circ$ X = I	% error
0	-537.2	-428.9	-238	-622.7	-15.9	-518.6	-20.9	-344.3	-44.7
1	-680.3			-714.8	-5.1	-612.9		-435.0	
2	-815.9		-497.9	-806.9	1.1	-707.1		-525.7	-5.6
3	-948.1	-829.7		-899.0	5.2	-801.3	3.4	-616.4	
5	-1148.5	-1051.4	-852.7	-1083.2	5.7	-989.7	5.9	-797.8	6.4
7	-1318	-1226.7	-1048.9	-1267.4	3.	-1178.2	4.0	-979.2	6.6
9			-1222.1	-1451.6		-1366.7		-1160.5	5.0
13			-1544	-1819.9		-1743.5		-1523.3	1.3
15	-1950	-1883		-2004.1	-2.8	-1931.9	-2.6	-1704	
21			-2176	-2556.7		-2497.2		-2248.9	-3.3

^a Columns 2–4 list the experimentally known NBS³⁶ data for $\Delta_f H^\circ(\text{InX}_3 \cdot n\text{NH}_3, \text{s})/\text{kJ} \cdot \text{mol}^{-1}$; columns 5, 7, and 9 give the SDR predictions for $\Delta_f H^\circ(\text{InX}_3 \cdot n\text{NH}_3, \text{s})/\text{kJ} \cdot \text{mol}^{-1}$; and columns 6, 8, and 10 give the percentage errors for these predictions.

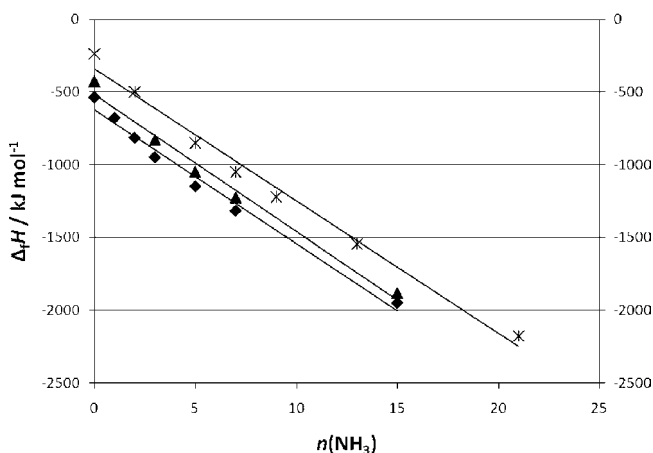


Figure 4. Plot of $\Delta_f H^\circ(\text{InX}_3 \cdot n\text{NH}_3, \text{s})/\text{kJ} \cdot \text{mol}^{-1}$ versus *n* for X = Cl (diamonds), Br (triangles), and I (stars) showing linear fit. See text for list of fitted linear equations.

for this system—than is obtained for the ammoniates as a family. Table 6 shows how the linear fits above reproduce the known experimental data. Reproduction of the parent data, $P(\text{InX}_3, \text{s})/\text{kJ} \cdot \text{mol}^{-1}$, is, however, seriously different (being between 16 and 45 %) from the NBS experimental data.

Since the plots in Figure 4 have a definite curvature, one can examine a polynomial fit (degree 2). Table 7 and Figure 5 show that this provides a much improved fit and, likely, a much better prediction of the data which is missing for the various intermediate ammoniates.

Table 7. Results for Quadratic SDR Plots for Ammoniates of Indium Trihalides, InX_3 (X = Cl, Br, I)^a

<i>n</i>	experimental			predictions and % errors					
	$\Delta_f H^\circ$ X = Cl	$\Delta_f H^\circ$ X = Br	$\Delta_f H^\circ$ X = I	$\Delta_f H^\circ$ X = Cl	% error	$\Delta_f H^\circ$ X = Br	% error	$\Delta_f H^\circ$ X = I	% error
0	-537.2	-482.9	-238	-554.8	-3.3	-438.3	2.2	-260.0	-9.2
1	-680.3			-682.4	-0.3	-568.3		-378.3	
2	-815.9		-497.9	-805.1	1.3	-693.5		-493.8	0.8
3	-948.1	-829.7		-922.8	2.7	-813.9	1.9	-606.5	
5	-1148.5	-1051.4	-852.7	-1143.2	0.5	-1040.1	1.1	-823.8	3.4
7	-1318	-1226.7	-1048.9	-1343.6	-1.9	-1247.0	-1.7	-1030.0	1.8
9			-1222.1	-1524.2		-1434.4		-1225.1	-0.2
13			-1544	-1825.5		-1751.2		-1582.4	-2.5
15	-1950	-1883		-1946.3	0.2	-1880.5	0.1	-1744.5	
21			-2176	-2189.1		-22152.2		-2164.5	0.5

^a Columns 2–4 list the experimentally known NBS³⁶ data for $\Delta_f H^\circ(\text{InX}_3 \cdot n\text{NH}_3, \text{s})$; columns 5, 7, and 9 give the SDR predictions for $\Delta_f H^\circ(\text{InX}_3 \cdot n\text{NH}_3, \text{s})$ and columns 6, 8, and 10 the percentage errors in these predictions.

The polynomial fits take the analytical form

$$\Delta_f H^\circ(\text{InCl}_3 \cdot n\text{NH}_3, \text{s})/\text{kJ} \cdot \text{mol}^{-1} = 2.490n^2 - 130.1n - 554.8 \quad (\text{Diamonds}, R^2 = 0.999)$$

$$\Delta_f H^\circ(\text{InCl}_3 \cdot n\text{NH}_3, \text{s})/\text{kJ} \cdot \text{mol}^{-1} = 2.422n^2 - 132.5n - 438.3 \quad (\text{Triangles}, R^2 = 0.999)$$

$$\Delta_f H^\circ(\text{InCl}_3 \cdot n\text{NH}_3, \text{s})/\text{kJ} \cdot \text{mol}^{-1} = 1.379n^2 - 119.7n - 260.0 \quad (\text{Stars}, R^2 = 0.999)$$

and from these results and Table 7 we note that:

(1) correlation coefficients are considerably improved compared to those for the linear SDR plots (Figure 4);

(2) errors in reproduction of *known* data are considerably less than those in Table 6 (except in a single instance) and rarely greater than 3 %;

(3) Table 7 is anticipated to provide reliable estimates for

$\Delta_f H^\circ(\text{InCl}_3 \cdot n\text{NH}_3, \text{s})$ for values of *n* = 4, 6, 8, 10–12,

14, 16–20, and possibly slightly beyond *n* = 21

$\Delta_f H^\circ(\text{InBr}_3 \cdot n\text{NH}_3, \text{s})$ for values of *n* = 1, 2, 4, 6, 8–14

$\Delta_f H^\circ(\text{InBr}_3 \cdot n\text{NH}_3, \text{s})$ for values of *n* =

1, 3, 4, 6, 8, 10–12, 16–20

(4) intercept terms are closer to the known³⁶ parent $\Delta_f H^\circ$ values with errors of -3.3 % (X = Cl); 2.2 % (X = Br), and -9.2 % (X = I);

(5) the nonlinearity for the ammoniates with *n* > 5 or 6 corresponds to continuously decreasing solvation enthalpy. This

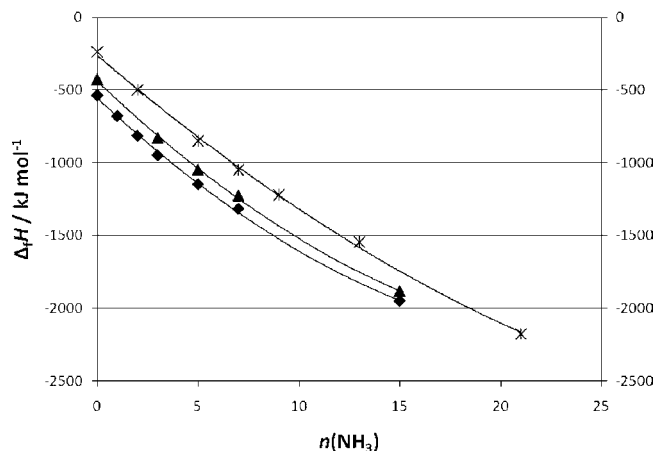


Figure 5. Plot of $\Delta_f H^\circ(\text{InX}_3 \cdot n\text{NH}_3, \text{s})/\text{kJ} \cdot \text{mol}^{-1}$ versus n for $X = \text{Cl}$ (diamonds), Br (triangles), and I (stars) showing polynomial fit (degree 2). See text for list of fitted quadratic equations.

contrasts markedly with the strict additivity which we have always observed for the hydrates. The strong interactions formed by water with the local environment give rise to the linear behavior observed in hydrates.

Significantly, the ammoniates also have the largest number ($n = 21$) of solvate molecules. Since, clearly, not all of these can be coordinated to the central ion this may cause deviations at higher values of n . Thus, the curvature in ammoniates could arise from at least two sources:

- the changing environment into which successive ammonia solvates are inserted, together with the relatively weak local interactions⁴⁵ between the molecules of both ammonia and solid solvate. The minimum enthalpy of incorporation of NH_3 into the solvate is observed⁴⁴ to be $-92.3 \text{ kJ} \cdot \text{mol}^{-1}$, a value which accords exactly with the average value found here for the indium trihalide ammoniates.

- an artifact of the data since these systems do not provide easy experimental thermochemistry. It seems worthwhile to suggest an experimental program to investigate these issues.

Other systems where $L \neq \text{NH}_3$ can be handled similarly, provided data exist. Examples are given below for cases where $L = \text{H}_2\text{S}$, $(\text{CH}_3)_2\text{S}$, and SO_2 .

Example 7. The NBS database³⁶ lists $\Delta_f H^\circ(\text{BeBr}_2, \text{s})/\text{kJ} \cdot \text{mol}^{-1} = -353.5$. What is the value predicted by SDR for $\Delta_f H^\circ(\text{BeBr}_2 \cdot 2\text{H}_2\text{S}, \text{s})/\text{kJ} \cdot \text{mol}^{-1}$?

From Table 1 in ref 4, $\theta_{\text{H}}(\text{H}_2\text{S})/\text{kJ} \cdot \text{mol}^{-1} \approx -53.6$, and since $n = 2$, so from eq 11

$$\Delta_f H^\circ(\text{BeBr}_2 \cdot 2\text{H}_2\text{S}, \text{s})/\text{kJ} \cdot \text{mol}^{-1} \approx -353.5 + 2(-53.6) = -460.7$$

The experimental value listed³⁶ is $-469 \text{ kJ} \cdot \text{mol}^{-1}$ (error 1.8 %).

Example 8. The NBS database³⁶ lists $\Delta_f H^\circ(\text{InBr}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s})/\text{kJ} \cdot \text{mol}^{-1} = -610.4$. What is the value predicted by SDR for $\Delta_f H^\circ(\text{InCl}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s})$? Can solvates other than those of $(\text{CH}_3)_2\text{S}$ be employed to make SDR estimates?

The solvent system $L = (\text{CH}_3)_2\text{S}$ has very few solvate examples for which data have been acquired. For this reason, making an SDR plot is not feasible. However, we can devise a plethora of various forms of eqs 12–16 inventively, to predict values for this and other solvents. Using NBS values exclusively, we have, using eq 13 in a general form

$$\begin{aligned} & \Delta_f H^\circ(\text{InCl}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s}) + \Delta_f H^\circ(\text{InBr}_3 \cdot n\text{NH}_3, \text{s}) \\ & \approx \Delta_f H^\circ(\text{InBr}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s}) + \Delta_f H^\circ(\text{InCl}_3 \cdot n\text{NH}_3, \text{s}) \end{aligned}$$

This equation, using values of $\Delta_f H^\circ(\text{InX}_3 \cdot n\text{NH}_3, \text{s})$ [$X = \text{Cl}, \text{Br}$] discussed earlier, leads to the following predictions for $\Delta_f H^\circ(\text{InCl}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s})/\text{kJ} \cdot \text{mol}^{-1}$: -728.9 (8.1 %, $n = 3$); -707.5 (5.0 %, $n = 5$); -701.7 (4.1 %, $n = 7$); and -677.4 (0.5 %, $n = 15$). Errors and degree of solvation, n , are given in parentheses. The errors are calculated using the NBS value of $-674.0 \text{ kJ} \cdot \text{mol}^{-1}$ cited³⁶ for $\Delta_f H^\circ(\text{InCl}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s})$.

Using eq 14 in the form

$$\begin{aligned} & \Delta_f H^\circ(\text{InCl}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s}) + \Delta_f H^\circ(\text{InBr}_3, \text{s}) \approx \\ & \Delta_f H^\circ(\text{InBr}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s}) + \Delta_f H^\circ(\text{InCl}_3, \text{s}) \end{aligned}$$

with parent salt data from NBS,³⁶ $-\Delta_f H^\circ(\text{InBr}_3, \text{s})/\text{kJ} \cdot \text{mol}^{-1} = -482.9$; $\Delta_f H^\circ(\text{InBr}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s})/\text{kJ} \cdot \text{mol}^{-1} = -610.4$, and $\Delta_f H^\circ(\text{InCl}_3, \text{s})/\text{kJ} \cdot \text{mol}^{-1} = -537.2$ leads to $\Delta_f H^\circ(\text{InCl}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s})$ predicted to be approximately $[-610.4 - 537.2 + 482.9] = -664.7 \text{ kJ} \cdot \text{mol}^{-1}$ (1.4 %).

A further approach, using eq 13 in the form

$$\begin{aligned} & \Delta_f H^\circ(\text{InCl}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s}) + \Delta_f H^\circ(\text{GaBr}_3 \cdot n\text{NH}_3, \text{s}) \\ & \approx \Delta_f H^\circ(\text{InBr}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s}) + \Delta_f H^\circ(\text{GaCl}_3 \cdot n\text{NH}_3, \text{s}) \end{aligned}$$

leads to the following results for $\Delta_f H^\circ(\text{InCl}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s})/\text{kJ} \cdot \text{mol}^{-1}$: -760.7 (12.8 %, $n = 1$); -738.1 (9.5 %, $n = 5$); -730.1 (8.3 %, $n = 6$); -725.9 (7.7 %, $n = 7$); and -727.6 (8.0 %, $n = 14$).

The involvement of hydrate data might normally be expected to lead to improved results. However, trivalent halides do not form hydrates readily and data are sparse. However, we can, for example, devise an equation using eq 16 in the form

$$\begin{aligned} & \Delta_f H^\circ(\text{InCl}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s}) + \Delta_f H^\circ(\text{MBr}_3 \cdot n\text{H}_2\text{O}, \text{s}) \\ & \approx \Delta_f H^\circ(\text{InBr}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s}) + \Delta_f H^\circ(\text{InCl}_3 \cdot n\text{NH}_3, \text{s}) \end{aligned}$$

where M represents a trivalent metal. For thallium chloride and bromide hydrates, thermodynamic data have been reported³⁶ for $\Delta_f H^\circ(\text{TlCl}_3 \cdot 4\text{H}_2\text{O}, \text{s})/\text{kJ} \cdot \text{mol}^{-1} = -1503$ and $\Delta_f H^\circ(\text{TlBr}_3 \cdot 4\text{H}_2\text{O}, \text{s})/\text{kJ} \cdot \text{mol}^{-1} = -1402$. Specifically

$$\begin{aligned} & \Delta_f H^\circ(\text{InCl}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s}) + \Delta_f H^\circ(\text{TlBr}_3 \cdot 4\text{H}_2\text{O}, \text{s}) \\ & \approx \Delta_f H^\circ(\text{InBr}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s}) + \Delta_f H^\circ(\text{TlCl}_3 \cdot 4\text{H}_2\text{O}, \text{s}) \end{aligned}$$

and thus $\Delta_f H^\circ(\text{InCl}_3 \cdot 2(\text{CH}_3)_2\text{S}, \text{s})/\text{kJ} \cdot \text{mol}^{-1} \approx [-610.4 - 1503 + 1402] = -711.4$ (5.5 %).

Finally, by considering SO_2 solvates, we can give an example of eq 15 in use. We can predict data for $\Delta_f H^\circ(\text{AlCl}_3 \cdot 2\text{SO}_2, \text{s})/\text{kJ} \cdot \text{mol}^{-1}$ using the SDR

$$\begin{aligned} & \Delta_f H^\circ(\text{AlCl}_3 \cdot 2\text{SO}_2, \text{s}) + \Delta_f H^\circ(\text{LiI} \cdot \text{SO}_2, \text{s}) \approx \\ & \Delta_f H^\circ(\text{LiI} \cdot 2\text{SO}_2, \text{s}) + \Delta_f H^\circ(\text{AlCl}_3 \cdot \text{SO}_2, \text{s}) \end{aligned}$$

Taking³⁶ $\Delta_f H^\circ(\text{LiI} \cdot \text{SO}_2, \text{s})/\text{kJ} \cdot \text{mol}^{-1} = -607.9$; $\Delta_f H^\circ(\text{LiI} \cdot 2\text{SO}_2, \text{s})/\text{kJ} \cdot \text{mol}^{-1} = -944.3$; and $\Delta_f H^\circ(\text{AlCl}_3 \cdot \text{SO}_2, \text{s})/\text{kJ} \cdot \text{mol}^{-1} = -1061.1$ leads to $\Delta_f H^\circ(\text{AlCl}_3 \cdot 2\text{SO}_2, \text{s})$ predicted to be $\approx [-1061.1 - 944.3 + 607.9] = -1398.0$ which agrees exactly with the value reported.⁴

Acknowledgment

One of us (HDBJ) would like to record his pleasure and his thanks to John Rowlinson for generously giving up time to discuss aspects of thermodynamics on a 1:1 basis and for his kind hospitality shown at Carlton House Terrace.

Supporting Information Available:

Excel spreadsheets ("Solver Example.xlsx" for Excel 2007 and "Solver Example.xls" for earlier versions) demonstrate the use of Excel Solver to optimize a set of additive contributions to a thermodynamic quantity as compared with a reference set. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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